Constraining industrial ammonia emissions using hyperspectral infrared imaging

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ABSTRACT

Atmospheric emissions of reactive nitrogen in the form of nitrogen dioxide (NO₂) and ammonia (NH₃) worsen air quality and upon deposition, dramatically affect the environment. Recent infrared satellite measurements have revealed that NH₃ emitted by industries are an important and underestimated emission source. Yet, to assess these emissions, current satellite sounders are severely limited by their spatial resolution. In this paper, we analyse measurement data recorded in a series of imaging surveys that were conducted over industries in the Greater Berlin area (Germany). On board the aircraft were the Telops Hyper-Cam LW, targeting NH₃ measurements in the longwave infrared at a resolution of 4 m and the SWING+ spectrometer targeting NO₂ measurements in the UV–Vis at a resolution of 180 m.

Two flights were carried out over German's largest production facility of synthetic NH₃, urea and other fertilizers. In both cases, a large NH₃ plume was observed originating from the factory. Using a Gaussian plume model to take into account plume rise and dispersion, coupled with well-established radiative transfer and inverse methods, we retrieve vertical column densities. From these, we calculate NH₃ emission fluxes using the integrated mass enhancement and cross-sectional flux methods, yielding consistent emissions of the order of 2200 t yr⁻¹ for both flights, assuming constant fluxes across the year. These estimates are about five times larger than those reported in the European Pollutant Release and Transfer Register (E-PRTR) for this plant. In the second campaign, a co-emitted NO₂ plume was measured, likely related to the production of nitric acid at the plant.

A third flight was carried out over an area comprising the cities of Staßfurt and Bernburg. Several small NH₃ plumes were seen, one over a production facility of mineral wool insulation, one over a sugar factory and two over the soda ash plants in Staßfurt and Bernburg. A fifth and much larger plume was seen to originate from the sedimentation basins associated with the soda ash plant in Staßfurt, indicating rapid volatilization of ammonium rich effluents. We use the different measurement campaigns to simulate measurements of Nitrosat, a potential future satellite sounder dedicated to the sounding of reactive nitrogen at a resolution of 500 m. We demonstrate that such measurements would allow accurately constraining emissions in a single overpass, overcoming a number of important drawbacks of current satellite sounders.

1. Introduction

The two principal forms of reactive nitrogen (Nr) emitted to the atmosphere are nitrogen dioxide (NO₂) and ammonia (NH₃). Tropospheric nitrogen oxides are emitted from fossil fuel combustion, vegetation fires, soil and lightning (Stavroukou et al., 2013). NH₃ is emitted into the atmosphere from biomass burning, oceans, soils, wild animals, industries, waste water treatment, fossil fuel combustion and domestic activities (Battye et al., 1994; Behera et al., 2013; Bouwman et al., 1997; Bray et al., 2018). The main source of NH₃, however, is agriculture (Sutton et al., 2013), which accounts for more than 80% of the total emissions in Europe (Pinterits et al., 2020), the United States (Bray et al., 2018) and China (Zhang et al., 2017). An important role is played by NH₃-based fertilizers, which are synthesized on a massive industrial scale, supporting the world’s need for food and...
feed (Erisman et al., 2008; Galloway et al., 2008). A large part of this produced NH$_3$ is lost to the atmosphere, through volatilization from synthetic fertilizer application and losses from livestock waste (Erisman et al., 2015).

Anthropogenic emissions of Nr strongly perturb the global nitrogen cycle, with devastating consequences for the environment. Deposition leads to a reduction of biodiversity through eutrophication and acidification of water and soils (Aneja et al., 2001; Dise et al., 2011; Erisman et al., 2013). Both NO$_x$ and NH$_3$ also contribute to the formation of particulate matter, deteriorating air quality, human health and life expectancy (Erisman et al., 2013; Lelieveld et al., 2015; Pope et al., 2009). While NO$_x$ emissions are declining worldwide (Georgoulias et al., 2019), atmospheric NH$_3$ levels are still increasing in most countries, with a recent study estimating increases of about 2% per year in Europe and the United States and 6% per year in East Asia (Van Damme et al., 2021). The issue is making its way on the international political agenda, but to successfully reduce worldwide NH$_3$ emissions and their environmental impacts, it is imperative that legislative action is supported by effective monitoring means.

Satellite observations of NH$_3$ have now become widely available, allowing analysis of the entire global atmospheric distribution of NH$_3$ and its temporal variability (e.g. Hickman et al. (2021), Shephard et al. (2020), Van Damme et al. (2021), Wang et al. (2021)). Using model assimilation and inversion, satellite data is being used to estimate regional and global NH$_3$ emission and deposition budgets (e.g. Chen et al. (2021), Evangelou et al. (2021), Kharol et al. (2018)). Other satellite-derived work relates to the study of individual NH$_3$ sources, such as animal farms and chemical fertilizer plants. To overcome the rather coarse spatial resolution (≥12 km) of the spaceborne Infrared Atmospheric Sounding Interferometer (IASI), Van Damme et al. (2018) exploited long term averages, and were able to identify and quantify the world's largest point emitters. They highlighted the importance of these on a global scale, and the fact that their emissions are significantly underestimated in state of the art bottom-up inventories. Follow-up work increased the number of identified global point sources to about 500 (Clarisse et al., 2019b) and estimated the atmospheric lifetime of NH$_3$ on a per site basis (Dammers et al., 2019). Despite the obvious progress that has been made, it has become clear that the limits are being reached on what can be done with existing satellite sounders. Indeed, their spatial resolution is much coarser than the typical size of an NH$_3$ point source, which makes the measurement of their emissions very challenging. Only the most important and isolated sources could be identified from space measurements and many smaller point sources, especially farms, were missed. Therefore, an effective monitoring of a species with a temporal and spatial variability as large as that of NH$_3$ requires an instrument capable of measuring at a much smaller spatial scale than that of IASI and other current hyperspectral infrared sounders.

It is in this context that a new satellite, called Nitrosat, has been proposed in answer to the 11th Earth Explorer Call from the European Space Agency (ESA). Nitrosat aims at mapping Nr on a global scale by measuring NO$_2$ and NH$_3$ in lowpass swaths of over 80 km at a spatial resolution of 500 m or below. This satellite would be launched in 2031 and would have a lifetime of at least three years. During this time frame, Nitrosat would observe the Earth simultaneously with other European missions such as CO2M, Sentinel 4 and Sentinel 5. All these missions are complementary and will provide improved measurements of NO$_2$ and NH$_3$, but none of them will come close to the spatial resolution provided by Nitrosat (Coheur et al., 2021).

In 2021, Nitrosat was selected to enter phase 0 (pre-development). To support the proposal and demonstrate what this satellite mission could offer, ESA is currently funding aircraft campaigns, called Nitrocam. Each flight aims at mapping NO$_2$ and NH$_3$ in an area of at least 10 by 15 km and across different source areas in Europe. The instruments on board are the UV–Vis SWING+ spectrometer developed by the Royal Belgian Institute for Space Aeronomy (BIRA-IASB) for observing NO$_2$ at a spatial resolution of about 180 m (Merlaud et al., 2018) and the commercial Telops infrared Hyper-Cam LW instrument, owned by German Research Center for Geosciences (GFZ), targeting NH$_3$ at a resolution of 4 m (Telops, 2022).

The present paper reports the results of a first series of Nitrocam flights over industries in the Greater Berlin area (Germany), with a focus on deriving industrial NH$_3$ emission rates. In the next section, we present the data measured in autumn 2020 over a fertilizer production facility in Piesteritz. An approach based on a hyperspectral range index (HRI) is used to detect the NH$_3$ plume emitted by the plant and its emission rates are derived using different complementary approaches. This includes a simulation of the measurements as they would be observed by Nitrosat. In Section 3, we report on two flights that took place in spring 2021, one over the same fertilizer plant of Piesteritz and the other over different types of industry near the cities of Staßfurt and Bernburg. In the last section we discuss the results in a wider context and summarize the main conclusions.

2. NH$_3$ measured by Hyper-Cam LW over Piesteritz in autumn 2020

The first Nitrocam flight took place on 8 October, 2020, between 10 and 11 AM (local time) near Piesteritz, Germany (51.88°N, 12.58°E), over an area of ~10 × 15 km$^2$ as shown in Fig. 1a. The target of the campaign was the Piesteritz fertilizer plant. It is the largest German production facility of NH$_3$ and urea, with a yearly production capacity over 1200 kt for both compounds (European Commission, 2007). The factory was earlier identified as an emission hotspot of atmospheric NH$_3$ (Clarisse et al., 2019b), and serves as a representative example of the main type of industrial NH$_3$ emitter.

For this flight, only the Hyper-Cam LW was operational. The Hyper-Cam LW (Lagueux et al., 2009a,b; Montembeault et al., 2010) is an imaging Fourier interferometer operating in the longwave infrared between 800 and 1350 cm$^{-1}$. Observing in nadir geometry, it combines a very high spatial resolution (4 m) with a medium spectral sampling (1.65 cm$^{-1}$). The instrument was mounted on the Telops' airborne platform and transported by the Cessna T207A aircraft to an altitude of 3 km. The area was surveyed by means of parallel, slightly overlapping swaths of about 1 km wide.

For each observation, we calculated the median brightness temperature over all spectral channels between 850 and 1100 cm$^{-1}$. The distribution of these temperatures is presented in Fig. 1b. Notable features are: the Elbe river, at a temperature around 286 K, slightly warmer than the surrounding fields, some very small clouds in the north-east and solar panels west from the industrial site, featuring brightness temperatures below 278 K. During the flight, the soil temperature increased several degrees, which can be seen from the west-to-east temperature gradient in the distribution.

2.1. Detection of NH$_3$

To attempt to detect NH$_3$ in the observed spectra, we used the so-called HRI or matched filter method, a close-to-optimal detection technique widely used both for NH$_3$ satellite observations (Whitburn et al., 2016), and hyperspectral imaging applications (Manolakis et al., 2016). The HRI is a dimensionless variable that quantifies the strength of the signal of a target compound (NH$_3$ in our case) in an observed spectrum, accounting for the expected spectral variability due to noise and the state of the surface and atmosphere. It can be interpreted as

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1. [https://www.esa.int/Applications/Observing_the_Earth/FutureEO/Preparing_for_tomorrow/Four_mission_ideas_toCompete_for_Earth_Explorer_11](https://www.esa.int/Applications/Observing_the_Earth/FutureEO/Preparing_for_tomorrow/Four_mission_ideas_toCompete_for_Earth_Explorer_11)
a generalized signal-to-noise ratio and is calculated, for each observed
spectrum $y$, as:

$$\text{HRI} = \frac{K^T S^{-1}_y (y - \bar{y})}{\sqrt{K^T S^{-1}_y K}}$$

(1)

with $\bar{y}$ and $S_y$ respectively the mean and covariance matrix of a
representative set of spectra containing background quantities of NH$_3$. $K$ is
the Jacobian of NH$_3$, calculated as the difference between two
spectra with different quantities of NH$_3$. By definition, the HRI has an
average of zero and a standard deviation of one on background spectra.
If the underlying distribution is normal, the HRI behaves like a z-score,
where a value above three indicates a probability higher than 0.99
that an enhanced NH$_3$ signature is present in the spectrum. In practice,
however, the distribution is rarely perfectly normal, and outliers are
common. When in doubt, a more robust spectral verification in the form
of spectral fitting or spectral whitening (De Longueville et al., 2021) is
called for. In what follows, we calculated the HRI in the 900–1000 cm$^{-1}$
spectral range, where the strongest NH$_3$ absorption features are located.

For the calculation of the mean spectrum and its associated co-
variance matrix, we used a recursive approach where first the mean
and covariance matrix are calculated on all spectra. This allows the
calculation of a preliminary HRI and removal of spectra containing
enhanced signatures of NH$_3$. Then, from the remaining spectra, a
second and final mean and covariance matrix are calculated (Clarisse
et al., 2019a). To reduce noise, we present here mostly averaged HRI
distributions (e.g., averaging 3 x 3 pixels yields a spatial distribution
at 12 m resolution, with a factor three improvement in the signal-to-
noise). In these distributions, the HRI is scaled in such a way that a
standard deviation of one is obtained over the background, so that the
HRI keeps its usual interpretation in terms of the z-score.

As shown in Fig. 1c, the distribution of the NH$_3$ HRI obtained in
this way reveals a large plume of NH$_3$ originating from the industrial
plant and extending over 7 km in the north-east direction. The spectra
measured over the solar panels were filtered out based on the median
brightness temperature (removing observations below 282 K), as they
led to false detections due to sharp emissivity features in the spectral
range of interest. This filter also served to remove the observations over
clouds. Apart from the main plume, which will be discussed in detail
further in the manuscript, large HRI values are found directly over the
industrial complex (Fig. 2c). Both large positive and large negative HRIs
are seen, respectively indicating dominant absorption and emission of
infrared radiation by NH$_3$. Note that for the calculation of the HRI, we
used a Jacobian that shows NH$_3$ in absorption hence from Eq. (1), NH$_3$
in absorption will result in a positive HRI while emission in a negative
one.

Examples of (averaged) spectra from both classes are shown in blue
in panels (d) and (e) of Fig. 2. These panels also display fitted synthetic
spectra (in red) obtained with a fitting model that adjusts the surface
temperature and the concentrations of the atmospheric constituents
to best match the observed spectrum (see next section). The differences
between the two (shown in green) have root mean squares values
(RMS) of 0.1 and 0.3 K. Withholding NH$_3$ from the fit leads to a
residual (orange) with large features of NH$_3$ (RMS) of 0.1 and 0.3 K.
Large positive residuals (in absorption) and large negative residuals
in emission will result in a positive HRI while emission in a negative
one.

Whether NH$_3$ is observed in absorption or emission depends on the
temperature difference between the background radiation (surface) and
the temperature of the NH$_3$ plume. This difference is more generally
known as the thermal contrast. With satellites, NH$_3$ is usually observed
in absorption during daytime, and in emission during nighttime when
thermal inversion is common (Clarisse et al., 2010, 2021). In the scene
under consideration, the differences in thermal contrast are largely
driven by the temperature of the different buildings and surface materi-
als. This becomes clear when we compare the HRI distribution (Fig. 2c)
with that of the temperature (Fig. 2b), and a Google Earth photograph of the corresponding area (Fig. 2a). Large positive HRIs can be discerned over several hot rooftops, whereas negative HRIs are observed over much colder storage tanks or silos. Note that thermal contrast not only determines the sign of the NH₃ signature, it also affects sensitivity of the observations to the target species, as a higher thermal contrast (in absolute value) leads to larger spectral signatures. This is particularly important for species located close to the surface (Bauduin et al., 2017), and is important for the discussion of the results in the next section.

The high spatial resolution of Hyper-Cam LW allows downsampling the measurements to various hypothetical satellite footprints as illustrated in Fig. 3 that shows HRI distributions computed at 200, 500 and 2000 m. The 200 and 500 m resolutions result in larger mean HRIs compared to the native measurements, allowing for a better visualization of the plume. For larger pixels, the plume becomes increasingly more dilute, and more difficult to attribute to the source. The resolution of 500 m shown on panel (b) corresponds to the resolution proposed for the Nitrosat candidate mission. While some of the finer detail is lost, at 500 m the plume can be seen with a good degree of spatial detail, enabling a straightforward identification of its source. This is immediately also the first demonstration that Nitrosat could measure, in a single overpass, an entire industrial plume of NH₃. In the next sections we show further that meaningful NH₃ concentrations and emission fluxes can be derived from such measurements.

2.2. Quantification of NH₃

To retrieve NH₃ vertical column densities from the measurements, we employed the optimal estimation method as implemented in the line-by-line radiative transfer code Atmosphit (Barret et al., 2005). The method iteratively minimizes the difference between the observed and the fitted spectrum (Rodgers, 2000), by adjusting the state of the surface and atmosphere, and allows simultaneously for the use of a priori information. The fitting range was set between 900 and 1000 cm⁻¹. NH₃ was given an a priori peak concentration of 200 ppb (450 ppb for the CSF-200 m retrieval for the non-rising plume, see the scenarios descriptions below) and a loose fitting constraint corresponding to 500% variability. The surface temperature, and total columns of water vapour (H₂O), ozone (O₃) and carbon dioxide (CO₂) were fitted with a variability of 30%. For the different species, total columns were fitted by uniformly scaling the a priori vertical profile. Vertical profiles of temperature, pressure and gas concentrations (except for NH₃, see below) were derived from ERA5 data from the European Centre for Medium-Range Weather Forecasts (Hersbach et al., 2020) and standard atmospheric models (Kneizys et al., 1996). For the radiative transfer calculations, the atmosphere was divided into 35 homogeneous layers between 0 and 3 km.

In what follows, we focus on the downwind plume, as retrievals over the factory itself are complicated by the large temperature gradients, inhomogeneous surface emissivities and the unknown temperature of the NH₃ gas close to the chimneys. For the downwind plume we assume a plume temperature equal to the ambient temperature. Mainly for computational reasons, rather than fitting each individual spectrum, we averaged the plume in 10 sections as shown in Fig. 4, leading to a reduction in spectral noise by a factor ~60 to 200 over a single spectrum.

Through the sensitivity to thermal contrast, the retrieval of the total column of NH₃ is dependent on the assumed plume altitude. As we cannot extract such information directly from the spectra (Clarisse et al., 2010), assumptions need to be made. Using a common plume model as detailed in Appendix, we consider two realistic, but contrasting scenarios. One of a non-rising plume (orange in Fig. 5a) and one of a
Fig. 3. NH₃ HRI distributions computed at spatial resolutions of (a) 200 m, (b) 500 m and (c) 2000 m centred on the fertilizer plant of Piesteritz (marked by an arrow on each panel) from the native data shown in Fig. 1c.

Fig. 4. Close-up of the NH₃ HRI distribution at 12 m resolution of Fig. 1c, illustrating the partitioning of the plume in 10 sections. In the bottom right corner of the figure are the NH₃ columns retrieved with the CSF method for the rising plume scenario displayed in blue in Fig. 5.

buoyant plume (blue in Fig. 5a). Both plumes are assumed to undergo vertical mixing at a rate typical for a stable atmosphere.

The 10 average spectra corresponding to the trapezoids in Fig. 4 were fitted assuming both of these profiles. The quality of the fits, with RMS values between 0.02 and 0.03 K, are even better than those shown in Fig. 2 since more spectra are averaged. From each column, a background column of 2.9 \(10^{15}\) molec cm\(^{-2}\) was subtracted, which was estimated independently from the mean of spectra measured outside of the plume. The resulting columns are shown in Fig. 5b and are seen to decrease with the distance from the source. This is logical as the plume disperses downwind over a larger area and as columns are expressed per surface unit. The large difference between the columns retrieved in the two scenarios originates from the dependence of the thermal contrast with the altitude: for a given quantity of NH₃, more thermal contrast leads to a larger spectral signature, and conversely, for a given spectral signature, assuming a larger thermal contrast/higher altitude in the retrieval, results in lower retrieved columns. Note that the retrieval uncertainty is larger at lower than at higher altitude, as in that case small uncertainties in the thermal contrast (e.g., due to small biases in the ERA5 temperature profiles) are relatively more important. This likely contributes to the larger fluctuations of the retrieved columns along the line of transport in the first scenario.

2.3. Flux retrievals

There exist several well-established algorithms for deriving point source emission fluxes from measurements of vertically integrated trace gas columns (Jacob et al., 2022; Theys et al., 2013). In the simplest case where the assumptions can be made of (i) a stationary emission flux, (ii) first order loss terms and (iii) a plume that is captured in full by the measurements, mass balance dictates (Seinfeld and Pandis, 2016):

\[ Q = \frac{M}{\tau}, \]

with \( Q \) the emission flux, \( M \) the total plume mass (minus background) and \( \tau \) the atmospheric lifetime of the species under consideration. The mass \( M \) should in this case be estimated from measurements within a sufficiently large box around the point source, so that transport out of the box can be neglected. As such, this method has been frequently applied to derive average emission fluxes from satellite measurements of short-lived species such as NO₂ (Beirle et al., 2011), SO₂ (McLinden
Fig. 5. (a) Two scenarios of plume rise and dispersion behaviour during transport downwind from the point source: non-rising (orange) and buoyant (blue). These two contrasting scenarios were modelled for a neutral atmosphere with an average wind speed of 7 m s\(^{-1}\) (see Appendix). The shaded areas represent \(h \pm 2 \sigma_z\). The values indicated on the right \(y\)-axis refer to the thermal contrasts between the surface and the parcel of air at the corresponding altitude indicated on the left axis. (b) \(\text{NH}_3\) column enhancements with respect to the background, retrieved by inversion of the 10 spectra defined in Fig. 4. The two curves correspond to the two plume rise assumptions shown in the upper panel. (c) Fluxes calculated with the IME (dashed lines) and the CSF (solid lines) methods from native data. Emission rates retrieved with the CSF method from data degraded at spatial resolutions of 200 m (dotted lines) and of 500 m (dash–dotted lines). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

et al., 2016), and \(\text{NH}_3\) (Van Damme et al., 2018). Several extensions and generalizations of the method exist, taking into account e.g. non-stationary fluxes and transport out of the box (Duncan et al., 2013). Here, we apply two complementary techniques particularly well applicable on high resolution aircraft measurements of individual plumes.

The first one is the integrated mass enhancement (IME) method (Frankenberg et al., 2016; Varon et al., 2018). It is suited for longer-lived species or when the downwind plume is only captured partially (as with aircraft measurements). The main idea of the method is replacing the atmospheric lifetime \(\tau\) with a residence lifetime \(\tau_{\text{res}}\) that represents the average lifetime of the pollutant in the observed plume, thereby taking into account deposition, transport out of the observation box and turbulent diffusion:

\[
Q_{\text{IME}} = \frac{M}{\tau_{\text{res}}} \quad (3)
\]

Using large eddy simulations, Varon et al. (2018) found the following empirical relation for the residence lifetime:

\[
\tau_{\text{res}} = L/(1.1 \log U + 0.6), \quad (4)
\]

with \(U\) the horizontal ambient wind speed and \(L\) the square root of the surface area of the observed plume.

The cross-sectional flux (CSF) method (also known as the traverse method) is another extension of the basic mass balance method. It allows reconstructing the flux history of sources whose emissions vary rapidly over time (Theys et al., 2013; Varon et al., 2018). The method works by dividing the plume into \(k\) different sections delimited by planes perpendicular to the surface and to the main wind direction (see Fig. 6). Relying on knowledge of the wind speed \(U_k\) in each slice, distances \(d_k\) downwind can be converted back into time \(t_k = \sum_{i=1}^{k-1} d_i/U_i\). Applying mass balance on a single slice between a distance \(d_k\) and \(d_{k+1}\) from the source, it is easy to see that the mean emission flux between a time \(-t_{k+1}\) and \(-t_k\) prior to the observation can be written as:

\[
Q_{\text{CSF}}(\Delta t_{k+1} \rightarrow \Delta t_k) = \frac{M_k}{\Delta t_k} e^{\tau_k}, \quad (5)
\]

with \(M_k\) the total mass in the slice \(k\) and \(\tau_k = t_{k+1} - t_k\) the time it takes for the plume to travel a distance \(d_k\).
Fig. 7. The top panel shows the NH$_3$ HRI distributions at 12 m resolution; the middle panel shows NO$_2$ columns over Staßfurt and Bernburg (from measurements performed on 09/05/21) and over Piesteritz (from data measured on 28/04/21) and the bottom panel depicts the NH$_3$ (circles) and NO$_2$ (triangles) sources catalogued in the E-PRTR inventory between 2009 and 2015. The sizes of these circles/triangles are indicators of the flux magnitudes.
factor $e^{\gamma/k}$ corrects for deposition and chemical losses. Here we assume a lifetime of 2 h for NH$_3$.

Both methods are easily applicable on the NH$_3$ columns presented in the previous section. First, for each of the 10 transects of the plume, the total columns are multiplied by the respective surface area and converted to a slice mass. The IME method is then simply applied on the sum of all slice masses, using an average wind speed of 7 m s$^{-1}$ estimated from ERA5 data. The application of the CSF method is equally straightforward using Eq. (5) and interpolated ERA5 wind speeds $U_k$. The results are detailed in Table 1 and shown on Fig. 5c with dashed (IME) and solid (CSF) lines. Both scenarios exhibit a decrease of fluxes over time (or an increase with distance) with the CSF method, but to a lesser extent in the higher altitude scenario. As we do not expect to observe a large variability of industrial emissions within 18 min (time taken for the plume to travel 7400 m downwind the source considering at an average wind speed of 7 m s$^{-1}$) this leads us to believe that there was at least some plume rise. It is also likely that the measurements have little or no sensitivity to the NH$_3$ located closest to the surface, with a thermal contrast barely above zero, resulting in an underestimation of the columns measured closest to the source. On the whole, we observe a good agreement between the IME and CSF flux estimates. The most plausible scenario (blue) provides a lower bound to the average flux of 60 g s$^{-1}$ equivalent to 1900 t yr$^{-1}$ if we consider constant emissions. According to the European Pollutant Release and Transfer Register (E-PRTR), atmospheric NH$_3$ emissions from this industrial complex amounts to 400 t yr$^{-1}$ (European Environment Agency, 2021), which is considerably lower than our estimate.

The high spatial resolution of the Hyper-Cam LW instrument makes it straightforward to apply the CSF method, as observations are easily attributed to a single transect. However, a future Nitrosat would fly at a considerably coarser resolution, with footprints not necessarily aligned with the transects. Fortunately, the method can easily be adapted. Suppose we have an observation grid $(i,j)$ as shown in Fig. 6, with retrieved cell masses $M_{ij}$. First a boolean plume mask $K_{ij}$ is established which flags all cells that are assumed to be part of the plume. In our case, this is done by setting a threshold value of 2 on the HRI. Next and similar as before, a number of appropriate transects are introduced perpendicular to the wind direction. For a given time slice $t_k$ the fractional overlap $P_{ij}(t_{k+1} \rightarrow t_k)$ is then calculated between each cell $(i,j)$ and the transect $k$. With this, the mass $M_k$ of the slice $k$ can be written as

$$M_k = \sum_{ij} P_{ij}(t_{k+1} \rightarrow t_k) M_{ij} K_{ij}$$

and Eq. (5) can be applied as before. The resulting emission rates are shown in Fig. 5c with dotted and dash-dotted lines from data degraded at spatial resolutions of 200 and 500 m, respectively. The fluxes obtained in this way are fully consistent with the ones obtained before, showing the consistency of the approach and the potential of a future Nitrosat to provide robust constraints on individual point source emitters in a single overpass of the instrument.

3. NH$_3$ measured by Hyper-Cam LW in spring 2021

A second campaign took place in the spring of 2021, with a flight over Piešťany on 28 April and a flight on 9 May over a large area that includes the cities Staßfurt and Bernburg. This second area was chosen as a target as it includes several different (industrial) sources of NO$_2$ and NH$_3$ according to the E-PRTR inventory (see bottom panel of Fig. 7).

Two instruments were on board the aircraft, which flew over the two areas at 3 km altitude: the Hyper-Cam LW, measuring NH$_3$ at a spatial resolution of 4 m and with a spectral sampling of 1.32 cm$^{-1}$ and the SWING+ instrument, measuring NO$_2$ at a spatial resolution of 180 m.

As for the first campaign presented in the previous section, an HRI was setup for the detection of NH$_3$. Since both spring flights used the same spectral sampling, a common mean spectrum and associated covariance matrix could be calculated. The resulting distributions are presented in the top panel of Fig. 7, as before degraded to a spatial resolution of 12 m. Before analysing the distributions in more detail, we note that the HRI background levels are higher for the Piešťany scene than for the Staßfurt/Bernburg area, indicating either higher background levels of NH$_3$ or higher thermal contrast. The HRI distributions measured by the satellite sounder IASI, shown in Fig. 8, confirm these results, and indicate that during both flights, enhanced levels of NH$_3$ were present over much of Germany. This background is likely related to fertilization of fields, which leads to a yearly peak in the NH$_3$ concentrations in spring over Europe (Paulot et al., 2014).

3.1. Piešťany

Just as in the first campaign, we observe a large plume coming from the Piešťany industrial complex, this time transported in north-west direction. While there are some other small local enhancements

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**Fig. 8.** NH$_3$ HRI distributions over Germany calculated from IASI measurements (on-board of Metop-B platform, from the morning overpass) whose pixel size and shape depend on the viewing angle of the instrument (Clerbaux et al., 2009). The different panels correspond to the data measured (a) on 08/10/20 (first flight over Piešťany), (b) on 28/04/21 (second flight over Piesteritz) and (c) on 09/05/21 (flight over the Staßfurt/Bernburg area). The black rectangles correspond to the surveyed areas. Pixels in grey are contaminated with clouds.
on the map, none of them could be attributed with a good degree of confidence to a specific source. We derived NH3 fluxes using the same procedure as before, with again two different assumed vertical dispersion models (see Fig. 9a and Appendix). Note that these profiles exhibit a larger vertical dispersion compared to the one in autumn-winter (autumn 2020 and spring 2021). The second part of the table shows the range of emission fluxes of NH3 from the fertilizer plant in Piesteritz retrieved with distinct approaches for the buoyant/non-rising plume.

As summarized in Table 1, the lower bounds on the derived fluxes are in good agreement, again indicating that the scenario of a buoyant plume, is the most likely one. The fluxes calculated with the IME method are lower than those calculated with the CSF technique because a longer lifetime is considered. Indeed, the residence lifetime defined by Eq. (4) takes into account the diffusion of NH3 in all directions while the CSF technique considers that transport occurs in a straight line. We also note that the relative difference between the fluxes calculated for the two scenarios is significantly smaller for the second (factor 2) than the first flight (factor 5), probably because of the better thermal contrast. This demonstrates that when the measurement conditions (thermal contrast) are better, the retrievals depend less on plume altitude assumptions.

As the SWING+ instrument was operational for this campaign we could also analyse its measurements. The instrument (Merlaud et al., 2018, 2020; Tack et al., 2019) is a compact whiskbroom imager dedicated to mapping NO2 and SO2 with the DOAS (Differential Optical Absorption Spectroscopy) technique (Platt and Stutz, 2008). SWING+ uses a UV–Vis spectrometer (Avantes ULS2048X64-EVO), an arduino-controlled scanner, a 7 × 100 μm bundle-slit fibre, and a PC. It records spectra between 280 and 550 nm at a spectral resolution of 0.8 nm FWHM (Full Width at Half Maximum). The typical sampling frequency is 2 Hz and the spatial resolution at 3 km altitude is 180 m. We analysed the spectra with the QDOAS software (Fayt et al., 2011), which retrieves the differential slant column densities (SCDs) of NO2 for each spectra relative to a reference spectrum of the same flight. The reference spectrum is an average of 25 spectra recorded over a clean area. The SCDs are converted to vertical column densities (VCDs) which retrieves the differential slant column densities (SCDs) of NO2 for each spectra relative to a reference spectrum of the same flight. The reference spectrum is an average of 25 spectra recorded over a clean area. The SCDs are converted to vertical column densities (VCDs) which retrieves the differential slant column densities (SCDs) of NO2 for each spectra relative to a reference spectrum of the same flight. The reference spectrum is an average of 25 spectra recorded over a clean area. The SCDs are converted to vertical column densities (VCDs) which retrieves the differential slant column densities (SCDs) of NO2 for each spectra relative to a reference spectrum of the same flight. The reference spectrum is an average of 25 spectra recorded over a clean area. 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Fig. 10. The central panel depicts the NH$_3$ HRI distribution at 12 m resolution over the Staßfurt/Bernburg (Germany) area (displayed on Fig. 7) superimposed on satellite visible imagery from Google Maps. The side panels provide close-up views on point sources detected over this area: (a) the soda ash plant of Staßfurt, (b) the wool production factory, (c) the Bernburg industry producing soda ash and (d) the sugar factory. The dotted box corresponds to the zone shown in Fig. 11.

Fig. 11. Close-up views over the settling ponds delimited by the dotted box in Fig. 10. From left to right, they show the brightness temperature distribution, the HRI distribution at 12 m resolution and a picture of the basins taken during the flight. The letters a, b and c point respectively to a transported plume, a cold part of the basin and a very hot part of the basin. They refer to the panels (a), (b) and (c) of Fig. 12.

3.2. Staßfurt and Bernburg

In this section, we present a qualitative analysis of the measurements over the Staßfurt/Bernburg area, which took place on Sunday 9 May 2021. Turbulent air made flying at a constant altitude and speed difficult, and this likely affected the measured spectra. It could be the reason why the agricultural sites included in the E-PRTR as NH$_3$ emitters and mapped in the bottom panel of Fig. 7 (green) were not seen. Nonetheless, combining analyses of the HRI distribution, together with the satellite visible imagery and the E-PRTR register led to several discoveries, which are illustrated on Fig. 10 and discussed below.

A clear plume is seen near a factory that produces mineral wool insulation (Fig. 10b). Production of such insulation is a known source of NH$_3$ (Battye et al., 1994), where it is used as a pH-regulator. Almost all of the NH$_3$ is released and emitted into the atmosphere at the end of the production process (Kowatsch, 2010). A small NH$_3$ plume is seen near a sugar industry south of Bernburg (Fig. 10d). Even though sugar factories are known to emit NH$_3$ (Chen et al., 2022), this site is not included...
in the E-PRTR inventory (bottom panel of Fig. 7). In order to confirm the validity of the HRIs, we applied a spectral whitening technique that allows exposing spectral enhancements (see De Longueville et al. (2021) for more information). The results, shown in Fig. 12, confirm irrefutably the validity of the NH₃ HRI enhancements highlighted in Fig. 10.

Small NH₃ plumes are observed directly over the chemical plants producing soda ash (Na₂CO₃) in Staßfurt (illustrated on panel (a)) and Bernburg (panel (c)). Within the Solvay process that is used to synthesize soda ash, NH₃ is a catalyst and is continuously recovered and reused. Yet, some emissions to air are unavoidable (Ecoys et al., 2009) as confirmed by our measurements. Just north of the Staßfurt plume there are several detections of NH₃ (indicated with an arrow in the central panel of Fig. 10), which could be transported NH₃ downwind from the Staßfurt plant, as no other nearby source was identified. The emissions from both soda ash plants are reported in the E-PRTR inventory amounting on average to 14 t yr⁻¹ for the Staßfurt plant and 300 t yr⁻¹ for Bernburg.

North of Staßfurt there is a large plume which seemingly originates from the large sedimentation basins associated with the soda ash plant, as shown in Fig. 11. The synthesis of soda ash produces wastewater with a very high fraction of suspended solids, that cannot be discharged as such. For this reason, settling ponds are operated to decant these solids. Several basins are used in parallel, with one basin receiving new effluents, while others are left to drain and dry completely (Freney et al., 1983). Unfortunately not within the surveyed area, so that no conclusions can be drawn on whether such emissions also occur at sedimentation basins of that plant.

These observations strongly suggest that the NH₃ plume originates from the warm fresh effluents. Its transport downwind north shows up in the HRI imagery either as NH₃ in emission or absorption depending on the underlying surface temperature. Given the fact that wastewater from soda ash production contains elevated quantities of dissolved ammonium (European Commission, 2007), it is not surprising that a significant amount is directly volatilized upon discharge. The elevated temperature and alkaline pH (Federal Environmental Agency, 2001; Steinhauser, 2008) of the effluent likely play a role, as these are two characteristics that highly favour volatilization of NH₃ (Cai, 1997; Freney et al., 1983).

As mentioned before, chimney stack exhausts, associated with soda ash production, are well-known to be a source of NOₓ emissions in the air (European Commission, 2007). However, to our knowledge it is the first time that NH₃ emissions are reported from a soda ash settling pond. As the HRI distributions suggest, the latter could be the dominant source of emissions from certain soda ash plants. Note that the sedimentation basins of the Bernburg soda ash plant were unfortunately not within the surveyed area, so that no conclusions can be drawn on whether such emissions also occur at sedimentation basins of that plant.

Among the various NH₃ plumes, only the largest one from Staßfurt can clearly be detected from the downsampled data at a resolution of 500 m, similar to what Nitrosat would observe (see Fig. 13b). The other plumes are mostly smaller than 500 m and once averaged over the entire pixel do not stand out from the background, highlighting the importance of the signal-to-noise ratio in the design of a future Nitrosat sounder. The 2000 m average (panel (c)) highlights a dramatic consequence of averaging, with an HRI over the sedimentation pond close to 0. In this case emission and absorption by NH₃ cancel each other completely, and retrievals over such a pixel would result in columns with a very large uncertainty (as both the HRI and thermal contrast are close to zero).

4. Discussion and conclusion

Airborne hyperspectral infrared observations of atmospheric NH₃ emissions have been reported before. Hulley et al. (2016) detected, among other species, NH₃ over a refinery and natural gas-fired power plant site in California with the Hyperspectral Thermal Emission Spectrometer (HyTES). The same instrument was used by Kuai et al. (2019) to detect and quantify NH₃ over a smouldering fire, a power plant and a large feedlot. Tratt et al. (2011, 2013) reported NH₃ measurements
of fumarolic vents and from sea-bird colonies in California. They also calculated NH$_3$ flow rates from the geothermal fumaroles field using a mass balance approach (Tratt et al., 2016). With this paper, we add to this list of observations, a production facility of synthetic NH$_3$, two soda ash plants, a mineral wool insulation factory and a sugar factory, as well as simultaneous observations of NH$_3$ and NO$_2$ plumes.

The observations over the fertilizer plant presented here, are particularly important as such plants are the single largest point source emitters of NH$_3$. Worldwide, over 250 such ultra-emitters have been identified using the existing landscape of satellite sounders (Clarisse et al., 2019b). However, these mostly concern isolated plants, and many plants located in industrial clusters or nearby other large sources remain unidentified due to the coarse spatial resolution (>10 km) of current satellite sounders. In addition, with large spatial gaps between adjacent observations, none of the current sounders offers imaging capability. Because of these limitations, long-term temporal averages are required for the identification of sources and derivation of emission fluxes. Furthermore, current spaceborne emission estimates come with very large uncertainties related to the difficulty in estimating background columns and the propagation of the uncertain knowledge of the atmospheric lifetime of NH$_3$ (Dammers et al., 2019; Van Damme et al., 2018).

As we have shown in this paper, most of these problems would be overcome with a satellite hyperspectral imager like Nitrosat, that offers a spatial resolution below 500 m. This resolution would be sufficient to observe, in a single overpass, an entire NH$_3$ plume emanating from an individual point source emitter. The background levels of NH$_3$ are in such measurements straightforwardly estimated, and because the plume can be observed at very short distances downwind, the lifetime problem is practically non-existent. We have demonstrated the consistency of the IME and CSF methods to derive emissions, using the native measurements and using simulated observational pixels of 200 and 500 m.

The remaining largest source of uncertainty of the emissions is the vertical profile of NH$_3$. Assumptions on the profile are required to take into account the dependence of the strength of the NH$_3$ spectral signal on the magnitude of the thermal contrast. In previous studies, vertical column densities were retrieved using fixed vertical profile assumptions. In this study, we have for the first time used dynamic vertical profiles, that vary with the distance downwind. Using two contrasting scenarios for plume rise we have shown that the retrieved emission fluxes can vary greatly. Fortunately, for larger thermal contrasts, as we saw with the spring-time flight over Piesteritz, the sensitivity to the assumptions becomes smaller. Furthermore, the differences between different plume rise scenarios are smaller very close or for distances far downwind the source, as can be seen from Fig. 9a. In the former case, plumes are still close to the chimney height, while in the latter case plumes become increasingly well-mixed throughout the vertical extent of the boundary layer. A future Nitrosat, with a foreseen swath of 80 km, will capture plumes much further downwind, and exploiting its high spatial resolution, emission estimates could be based on the part of the plume furthest downwind. Another idea that could be explored is to retrieve altitude information directly from the measurements by assuming steady-state emissions, i.e. what vertical plume rise assumption would yield a constant emission flux?

While Nitrosat targets both NO$_2$ and NH$_3$, the focus of this paper has been on NH$_3$ measurements as several other demonstration campaigns previously highlighted the advantage of high spatial resolution measurement for NO$_2$ source identification and quantification (Fujinawa et al., 2021; Meier et al., 2017; Souri et al., 2018). As an example, the measurements presented in Tack et al. (2021) convincingly demonstrate that a spatial resolution of less than 1 km is required to identify and separate individual point sources in the industrial cluster of Antwerp harbour (Belgium). In the present study however, we showed the first example of large simultaneous emissions of NO$_2$ and NH$_3$.

The campaign over the Staßfurt/Bernburg area proved to be very interesting with the discovery of the large NH$_3$ emissions fluxes from the sedimentation basins of the soda ash plant in Staßfurt. Several other and smaller industrial plumes were seen as well, similar in size as the ones previously seen by HyTES. Such smaller plumes only cover one or two measurement pixels of a future Nitrosat. However, nothing would prevent also in this case to estimate emission fluxes using e.g. the IME method. Attributing the precise source of these to specific industrial processes would also be straightforward in regions where industries are well spread out. However, in larger industrial clusters, with many potential emitters, identification of smaller sources would prove more challenging and would require temporal averaging or the use of third party information on the type of activities carried out.

Using HyTES, Kuai et al. (2019) were able to capture large NH$_3$ plumes directly over the feedlots in the U.S. However, transport over longer distance (>500 m) was not reported, nor was the derivation of emission fluxes. What is currently missing in terms of Nitrosat demonstration, is comprehensive and representative survey flights over agricultural areas, together with a demonstration that agricultural emission fluxes can be retrieved in a complex landscape of smaller sources. For this reason, in the summer of 2022 several flights took place over the Po Valley in Italy, the largest NH$_3$ hotspot region in Europe and home to many small and large farms. The analysis of the results of the campaign are underway and will be subject of a follow-up study.
CRediT authorship contribution statement

Lara Noppen: Conceptualization, Writing – original draft, Analysis, The column and flux retrievals, Prepared the figures, Campaign planning, Revision of the manuscript, Interpretation of the results.

Lieveen Clarisse: Conceptualization, Writing – original draft, Campaign planning, Revision of the manuscript, Interpretation of the results.

Frederik Tack: Responsible for the NO\textsubscript{2} measurements, Campaign planning, Revision of the manuscript, Interpretation of the results.

Thomas Ruhzt: Organized the campaigns, Carried out the measurements, Campaign planning, Revision of the manuscript, Interpretation of the results.

Dirk Schuette-meyer: Campaign planning, Revision of the manuscript, Interpretation of the results.

Lara Noppen: Conceptualization, Writing – original draft, Analysis, The column and flux retrievals, Prepared the figures, Campaign planning, Revision of the manuscript, Interpretation of the results.

Alexis Merlaud: Responsible for the NO\textsubscript{2} measurements, Campaign planning, Revision of the manuscript, Interpretation of the results.

Michel Van Roozendael: Responsible for the NO\textsubscript{2} measurements, Campaign planning, Revision of the manuscript, Interpretation of the results.

Martin Van Damme: Conceptualization, Writing – original draft, Campaign planning, Revision of the manuscript, Interpretation of the results.

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Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The data that has been used is confidential

A.1. The Gaussian plume model

Assuming homogeneous steady-state winds and a steady-state point source, plume behaviour can be described with a Gaussian plume dispersion model, which as a formal solution to the advection-diffusion equation, takes into account both advection and atmospheric diffusion (Stockie, 2011). Neglecting the reflection from the ground and from the planetary boundary layer (PBL), the solution can be written as:

\[
C(x, y, z) = \frac{Q}{2\pi\sigma_x\sigma_y U} e^{-\frac{2}{\sigma_x^2} - \frac{2}{\sigma_y^2}},
\]

where \(C(x, y, z)\) is the concentration at the position specified by the downwind \((x)\), crosswind \((y)\) and vertical \((z)\) directions, \(Q\) the source flux rate, \(U\) the horizontal wind speed and \(h(x)\) the central height \(h\) of the plume as a function of its distance downward from the source \(x\). The standard deviations \(\sigma_x(x)\) and \(\sigma_y(x)\) describe the horizontal and vertical spreads of the plume along the \(y\) and \(z\) axis. In case of vertical integrated measurements, all that matters is the shape of the vertical profile. For our retrieval, we can therefore use the following reduced form of Eq. (7):

\[
C(x, z) = C_{\text{peak}} e^{-\frac{(z-h)^2}{2\sigma_z^2}},
\]

with \(C_{\text{peak}}\) the a priori peak concentration. This equation has two unknowns, the central plume height \(h\), and the vertical spread \(\sigma_z\), which we now parametrize.

A.2. Advection and initial plume rise

At least initially, a plume often undergoes vertical transport, as a result of either its initial momentum, or its buoyancy, in case the emitted gas is hotter or less dense than the surrounding air. A common model for the central height \(h\) of a plume as a function of its distance downwind from the source \(x\), the horizontal wind speed \(U\) and the initial buoyancy flux \(F\) is (De Visscher, 2014; Hanna et al., 1982):

\[
h(x) = h_0 + \frac{1.6 F^\frac{1}{3} x^2}{U},
\]

where \(h_0\) is the initial height at the source. This relationship is known as the ‘2/3 law’ and is in agreement with the majority of field and laboratory data. The coefficient 1.6 is considered accurate within a range of ±40% whose variations are due to down-wash or local ground effects (Hanna et al., 1982). It is for example assumed to be 2 by Briggs (1965).

The buoyancy flux \(F\) depends on several factors such as the density, temperature and initial efflux velocity of the gas at the chimney and the radius of the stack, all of which we do not know. One scenario that we can exclude is that of very hot plumes, which would result in negative thermal contrast and negative HRIs. As these were not observed in any of the industrial plumes, we conclude that the initial buoyancy must be driven by its initial momentum and/or differences in density. For the study cases presented in Sections 2 and 3.1, we assumed both a small and a large value for \(F\) (5 and 1000 m\(^4\) s\(^{-3}\)).

However, plumes do not rise indefinitely but reach a maximum altitude referred to as the final plume rise height (Willis and Deardorff, 1983). This altitude is reached at a distance \(x_f\) downwind from the source that approximately satisfies (De Visscher, 2014):

\[
\begin{align*}
x_f &= 49 F^\frac{1}{3} & \text{for } F < 55 \text{ m}^4 \text{ s}^{-3} \\
x_f &= 119 F^\frac{1}{3} & \text{for } F > 55 \text{ m}^4 \text{ s}^{-3}
\end{align*}
\]

At distances greater than \(x_f\), the altitude of the plume remains constant.

A.3. Diffusion

Plumes undergo vertical and horizontal mixing due to atmospheric turbulence, generated by buoyant air parcels and wind shear (Gulliver, 2012; Willis and Deardorff, 1983). The amount of diffusion varies greatly depending on the atmospheric conditions. The Pasquill–Gifford classification describes and classifies the stability of the boundary layer in six classes based on the surface wind speed, the sun insulation and the cloud cover (Gifford, 1961; Pasquill, 1961). The classes are: very unstable (A), unstable (B), slightly unstable (C), neutral (D), slightly stable (E) and stable (F).

In the Gaussian plume model, diffusion is characterized by the horizontal and vertical spread \(\sigma_x\) and \(\sigma_z\). Here, we follow Martin (1976), who parametrized these in terms of stability classes as:

\[
\begin{align*}
\sigma_x(x) &= ax^b \\
\sigma_z(x) &= cx^d + f
\end{align*}
\]

where \(a, h, c, d\) and \(f\) are constants defined for each stability class.

For the study cases presented in Sections 2 and 3.1, the atmospheres can be considered, respectively, as neutral (D) and slightly unstable (C) according to the wind speed from ERA5 data and the sun insulation.